# Immigration Policy in a Time of Secular Stagnation

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#### Overview

Significant demographic transition in the US over last century

Macroeconomic implications - Secular Stagnation

 Fiscal consequences - Social Security, Government Debt, Monetary Policy

Focus on immigration as an economic policy instrument

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# **Empirical Overview**

Value	'75-'85	'08-'18
RGDP Growth	3.2%	1.5%
Investment Growth	5.0%	2.7%
Net Worth/GDP	251% <sup>1</sup>	372%
Interest Rates	2.91%	0.86%

# Mechanism

Rise in life expectancy, decline in birth rate

 Relative rise in share of households nearer to peak of life-cycle wealth

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Rise in wealth relative to output

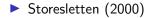
Declining interest rates

# Related Literature

Eggertsson, Lancastre, Summers (2018)

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Ariby, Geppert, Ludwig (2017)



### Questions

To what extent can immigration policy resolve demographic imbalances?

▶ How much can skilled immigration improve economic growth?

▶ How much immigration would it take to reach 4% growth?

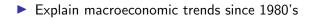
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How can immigration impact the fiscal outlook?



Present a model accounting for demographics (age, education)

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Evaluate counterfactual immigration policies

# Model Overview

Standard OLG, production economy

Two types - high/low productivity

Linear income tax per type

Cohort-dependent birth rates and survival rates

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Historical immigration rates by education

# Agent Optimization

Agent of cohort j with education e at time t solves:

$$V_{j,t}(a_{j,t}) = \max_{c_{j,t}, n_{j,t}, a_{j,t+1}} \frac{\left(c_{j,t}^{\gamma} (1 - n_{j,t})^{1 - \gamma}\right)^{1 - \sigma}}{1 - \sigma} + s_{j,t} \beta V_{j,t+1}(a_{j,t+1})$$
(1)

s.t. 
$$c_{j,t} = w_t \epsilon_e z_{t-j+1} n_{j,t} + (1+r_t) a_{j,t} - a_{j,t+1} - \phi_e(\cdot)$$
 (2)

$$\phi_{e}(\cdot) = \tau_{e} \left( w_{t} \epsilon_{e} z_{t-j+1} n_{j,t} + r_{t} a_{j,t} \right)$$
(3)

and 
$$a_{j,j+J+1} \ge 0$$
, (4)

# Firm Optimization

Firms solve:

$$\max_{K_t, L_t} K_t^{\alpha} \left( A_t L_t \right)^{1-\alpha} - (r_t + \delta) K_t - w_t L_t$$
(5)

#### Optimality conditions:

$$r_t = \alpha \left(\frac{\kappa_t}{A_t L_t}\right)^{\alpha - 1} - \delta \tag{6}$$

$$w_t = (1 - \alpha) \left(\frac{K_t}{A_t L_t}\right)^{\alpha}.$$
 (7)

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### Government

Aggregate tax revenue:

$$\Phi_t = \sum_{j=t}^{t-J+1} \sum_{e \in \{h,l\}} \mu_{j,t}^e \phi_e(\cdot).$$
(8)

Government budget constraint:

$$G_t = \Phi_t + B_t, \tag{9}$$

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# Equilibrium

# Dynamic general equilibrium: prices $\{w_t, r_t\}$ and quantities $\{c_{j,t}^*, n_{j,t}^*, a_{j,t+1}^*\}$ such that:

- 1. Given prices and government policy, agents choices satisfy Equation 1 Equation 4,
- 2. Prices are determined in competitive markets according to Equation 6 and Equation 7,
- 3. Markets clear:

$$K_t = \sum_{j=t}^{t-J+1} \sum_{e \in \{h,l\}} \mu_{j,t}^e a_{j,t+1}$$

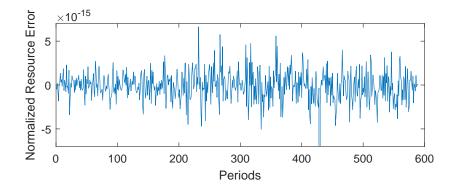
$$L_t = \sum_{j=t}^{t-J+1} \sum_{e \in \{h,l\}} \mu_{j,t}^e e_{Z_{t-j+1}} n_{j,t}$$

$$Y_t = C_t + K_{t+1} - (1-\delta) K_t + G_t$$

- 4. Government budget constraint (9) is satisfied.
- 5. Accidental bequests received by the government are determined according to

$$B_{t} = \sum_{j=t}^{t-J+1} \sum_{e \in \{h,l\}} (1-s_{j,t}) \mu_{j,t}^{e} a_{j,t+1}.$$
(10)

# Equilibrium Error



$$\mu_{j,t+1}^e = \mathbf{s}_{j,t} \mu_{j,t}^e \tag{11}$$



$$\tilde{\mu}_{j,t+1}^{e} = s_{j,t} \tilde{\mu}_{j,t}^{e} + m_{j,t+1}^{e}$$
(12)

► Population:

$$M_{t} = \sum_{j=t}^{t-J+1} \sum_{e \in \{h,l\}} \left( \mu_{j,t}^{e} + \tilde{\mu}_{j,t}^{e} \right)$$
(13)

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Native newborns:

$$\sum_{e \in \{h,l\}} \mu_{t+1,t+1}^e = \zeta_t M_t \tag{14}$$

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-  $\zeta_t$  is the birth rate at time t.

- Education shares determined by education rates by cohort.

#### Immigrants:

$$\sum_{e \in \{h,l\}} m_{j,t}^e = \psi_t \lambda_{j,t} M_t \tag{15}$$

#### - $\psi_t$ is the immigration rate at time t.

- Education shares determined by immigrant education rates by year.

Define relative population at time t as:

$$\left\{\frac{\sum_{e\in\{h,l\}} \left(\mu_{j,t}^{e} + \tilde{\mu}_{j,t}^{e}\right)}{M_{t}}\right\}_{j=t}^{t-J+1}$$
(16)

Population is relatively stable if ∀ ε > 0 ∃ t(ε) > 0 such that t > t(ε) ⇒

$$\max\left\{ \left| \left\{ \frac{\sum_{e \in \{h,l\}} \left( \mu_{j,t}^{e} + \tilde{\mu}_{j,t}^{e} \right)}{M_{t}} \right\}_{j=t}^{t-J+1} - \left\{ \frac{\sum_{e \in \{h,l\}} \left( \mu_{j,t}^{e} + \tilde{\mu}_{j,t}^{e} \right)}{M_{t}} \right\}_{j=t+1}^{(t+1)-J+1} \right| \right\} < \varepsilon$$
(17)

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# **Computing Population Dynamics**

1. Using earliest available data, find relatively stable population.

2. Allow demographics to change over the transition.

3. Iterate until new relatively stable population (and stable prices) reached.

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### Parameters

Parameter	Symbol	Value
Coefficient of Relative Risk Aversion	σ	3
Consumption Share of Utility	$\gamma$	0.65
Discount Factor	β	1.025
Maximum Age	J	120
Capital Share	α	0.36
Depreciation Rate	δ	0.085
Labor Productivity Growth Rate	g	0.015
Education Premium	$\epsilon_{e}$	170%
Tax Rate - college not attained	$ au_l$	6.2%
Tax Rate - college attained	$ au_{h}$	12.1%

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# Implementing Demographics

Total Change horizon: 1900-2095

Assume initial value is true dating back to 1900

Allow historical values to change over transition

 Integrate available projections (e.g., birth rates from Census Bureau)

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# Assumptions

Age distribution of entrants equals cross sectional age distribution in 2017.

Birth rate per year is common to all types.

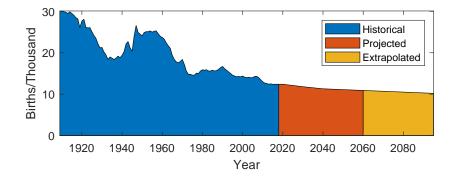
Children of immigrants draw from native college attainment distribution.



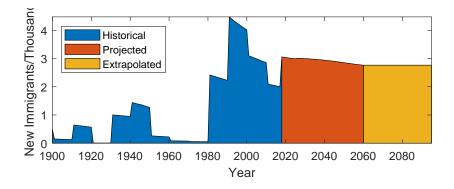
Capital of immigrants is the same as natives, per type.

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# **Birth Rates**

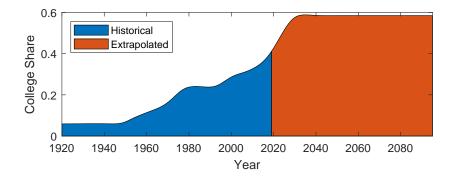


# Immigration Rates



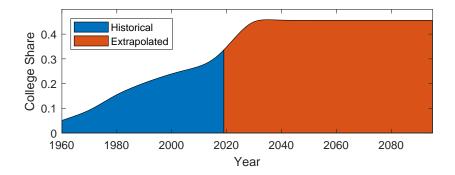
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# Education Rates: Natives



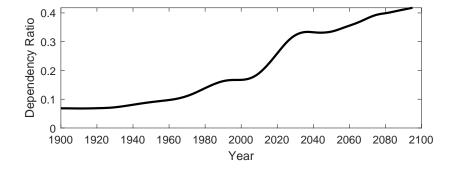
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# Education Rates: Immigrants



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### Dependency Ratio



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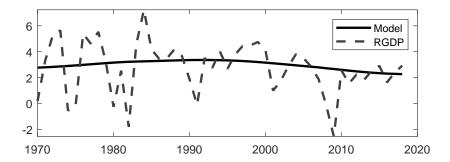
# Computing Equilibrium Path

► Value function iteration + iterating over K/L ratio

 Problem: Don't want to shock the economy with changing demographics.

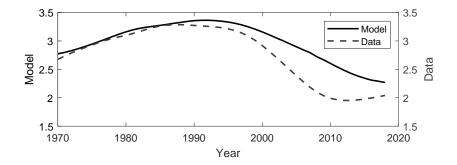
Solution: Add more initial periods until economy is "stationary" over the first N periods.

# Baseline Economy: Economic Growth



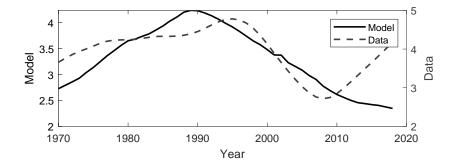
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#### Baseline Economy: Economic Growth



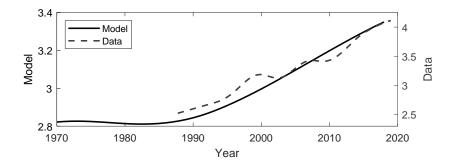
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# Baseline Economy: Investment Growth



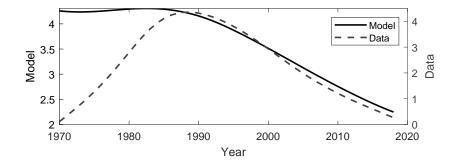
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Baseline Economy: Capital-to-Output



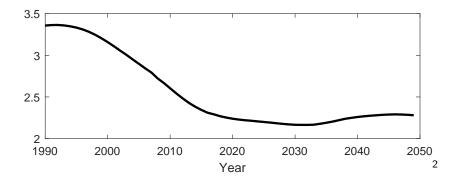
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# Baseline Economy: Real Interest Rates



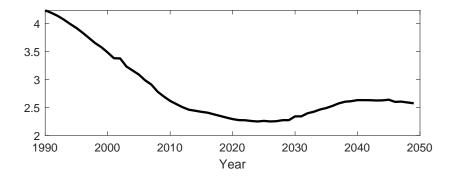
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#### Baseline Projection: Economic Growth



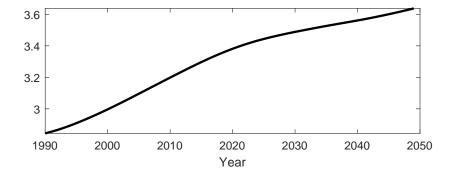
<sup>2</sup>LR: Population Growth = 0, Econ Growth Rate =  $g \rightarrow \langle \overline{g} \rightarrow \langle \overline{z} \rightarrow \langle$ 

# Baseline Projection: Investment Growth



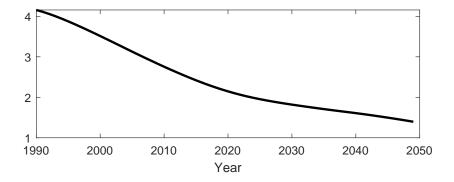
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# Baseline Projection: Capital-to-Output



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# Baseline Projection: Real Interest Rates



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# Counterfactual #1

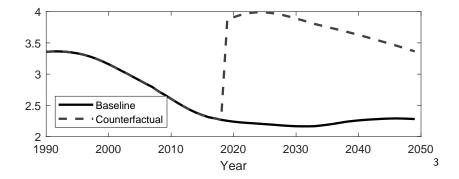
• Increase the immigration rate by 4  $\times$  baseline

#### ► Mathematically:

$$\sum_{e \in \{h,l\}} m_{j,t+1}^e = 4\psi_t \lambda_{j,t} M_t \tag{18}$$

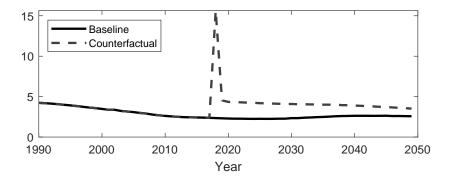
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## Counterfactual #1: Economic Growth



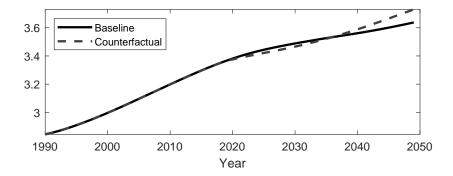
<sup>3</sup>LR: Population Growth = 1.15%, Econ Growth Rate = 265%  $\rightarrow 42\%$   $\rightarrow 2\%$ 

## Counterfactual #1: Investment Growth



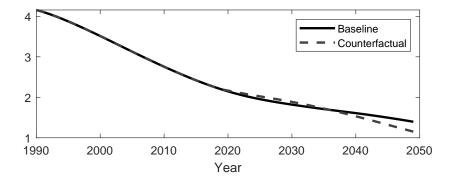
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# Counterfactual #1: Capital-to-Output



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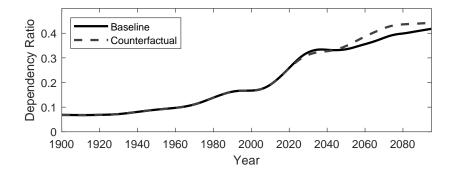
#### Counterfactual #1: Real Interest Rates



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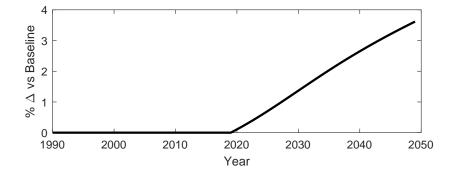
## Counterfactual #1: Dependency Ratio



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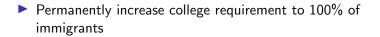
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Counterfactual #1: Taxes-to-Output



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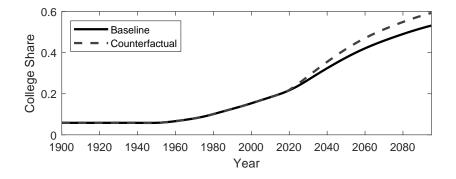
# Counterfactual #2



Gives an upper bound of skill requirement effect

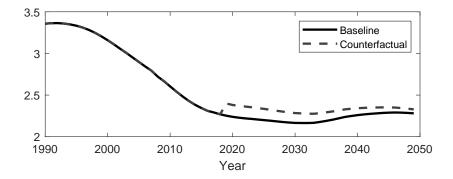
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## Counterfactual #2: College Share



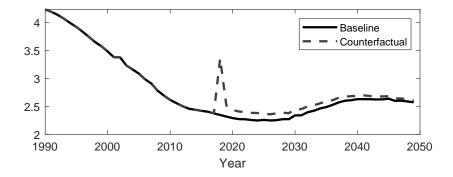
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## Counterfactual #2: Economic Growth



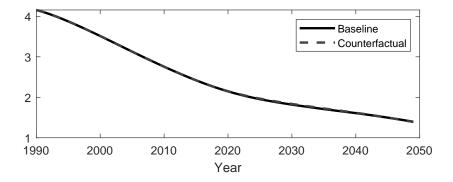
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## Counterfactual #2: Investment Growth



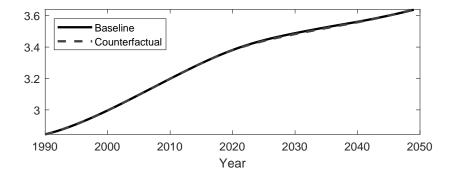
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#### Counterfactual #2: Real Interest Rates



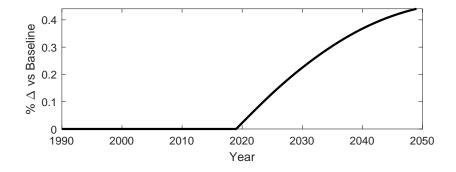
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## Counterfactual #2: Capital-to-Output



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Counterfactual #2: Taxes-to-Output



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## Conclusion

 Increased immigration rates might not resolve demographic imbalances.

Immigration could possibly alleviate budget issues - requires significant immigration and little corresponding government expenditures.

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• 4% growth is possible through  $4 \times$  immigration rate.

## Future Work

Improve demographics - e.g., birth rates by type, and data inputs

Get more out of the model and understand the mechanism

Richer fiscal policy - e.g., Social Security and government debt

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Evaluate alternative assumptions

# **Remaining Questions**

Are prices really determined in a "closed" economy?

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What are the consequences of rising debt?