## The Cost of Uncertainty about the Timing of Social Security Reform

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• Language: "structural uncertainty" and "timing uncertainty."

• Our contribution: new methodology for dynamic problems with timing and structural uncertainty.

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• Feature 1: Explicitly model timing uncertainty.

In contrast to "timing premium" literature: Epstein, Farhi, and Strzalecki (2014, AER), Blundell and Stoker (1999, EER), Eeckhoudt, Gollier, and Treich (2005, EER).

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- Feature 2: (Non) stationary distributions of timing risk. Unlike standard stochastic DP: uncertainty is Markov (stationary).
- Feature 3: Developed to evaluate policy questions.

Study specific examples of policy-induced uncertainty (Baker, Bloom, and Davis (2013) and others).

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- To stay solvent: benefits  $\downarrow 21\%$ , or taxes  $\uparrow 3.1$  points, or...
- Everyone knows reform is coming, but when? & how?

"The rational expectations equilibrium concept common to all of our models requires...that an agent living within one of these models would know the monetary and fiscal policies affecting him." —Sargent. For example: literature on feasibility/optimality of SS reforms in macro (Kitao (2014), McGrattan and Prescott (2014)).

# Standard (deterministic) regime switching

$$\max_{u(t)_{t\in[0,T]}} : J = \int_0^{t_1} f_1(t, u(t), x(t)) dt + \int_{t_1}^T f_2(t, u(t), x(t)) dt,$$

subject to

$$\frac{dx(t)}{dt} = g_1(t, u(t), x(t)), \text{ for } t \in [0, t_1],$$
$$\frac{dx(t)}{dt} = g_2(t, u(t), x(t)), \text{ for } t \in [t_1, T],$$
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$$x(0) = x_0, \ x(T) = x_T,$$
$$t_1 \text{ and } g_2() \text{ are known.}$$

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## Our stochastic version

$$\max_{u(t)_{t \in [0,T]}} : J = \mathbb{E}_{t_1,\alpha} \left[ \int_0^{t_1} f_1(t, u(t), x(t)) dt + \int_{t_1}^T f_2(t, u(t), x(t)) dt \right],$$

subject to

$$\frac{dx(t)}{dt} = g_1(t, u(t), x(t)), \text{ for } t \in [0, t_1],$$
$$\frac{dx(t)}{dt} = g_2(t, u(t), x(t)|\alpha), \text{ for } t \in [t_1, T],$$
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 $t_1$  and  $\alpha$  are stochastic,

 $t_1$  density  $\phi(t_1)$  with support  $[0, \infty]$ ,  $\alpha$  density  $\theta(\alpha)$  with support [0, 1].

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**Theorem (Necessary Conditions).** The necessary conditions can be derived recursively in two steps.

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Step 1. Solve the post-switch subproblem  $\forall (t_1, \alpha)$ : The program  $(u_2^*(t|t_1, x(t_1), \alpha), x_2^*(t|t_1, x(t_1), \alpha))_{t \in [t_1, T]}$  solves a fixed endpoint Pontryagin subproblem

$$\max_{u(t)_{t \in [t_1, T]}} : J_2 = \int_{t_1}^T f_2(t, u(t), x(t)) dt,$$

subject to

$$\frac{dx(t)}{dt} = g_2(t, u(t), x(t)|\alpha), \text{ for } t \in [t_1, T],$$
  
$$t_1 \text{ given, } \alpha \text{ given, } x(t_1) \text{ given, } x(T) = x_T.$$

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#### Step 2. Solve the pre-switch subproblem:

The program  $(u_1^*(t), x_1^*(t))_{t \in [0,T]}$  solves a fixed endpoint Pontryagin subproblem with continuation function  $\mathcal{S}(t, x(t), \alpha)$ :

$$\max_{u(t)_{t\in[0,T]}} : J_1 = \int_0^T \left[ \int_t^\infty \phi(t_1) dt_1 \right] f_1(t, u(t), x(t)) dt + \int_0^T \int_0^1 \theta(\alpha) \phi(t) \mathcal{S}(t, x(t), \alpha) d\alpha dt,$$

subject to

$$\begin{aligned} \mathcal{S}(t, x(t), \alpha) &= \int_{t}^{T} f_{2}(z, u_{2}^{*}(z|t, x(t), \alpha), x_{2}^{*}(z|t, x(t), \alpha)) dz, \\ &\frac{dx(t)}{dt} = g_{1}(t, u(t), x(t)), \text{ for } t \in [0, T], \\ &x(0) = x_{0}, \ x(T) = x_{T}. \end{aligned}$$

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-21% benefit cut.

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-3.1 point tax increase.

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• In other words, households know which of the two worlds they are living in:

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• Current policy is  $(\tau_1, b_1)$  and post-reform policy is  $(\tau_2, b_2)$ .

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$$\max_{c(t)_{t\in[0,T]}} : J = \mathbb{E}\left[\int_0^T e^{-\rho t} \Psi(t) u(c(t)) dt\right], \quad \text{subject to:}$$
$$\frac{dk(t)}{dt} = rk(t) + y_1(t) - c(t), \text{ for } t \in [0, t_1],$$

$$\frac{dk(t)}{dt} = rk(t) + y_2(t) - c(t), \text{ for } t \in [t_1, T],$$

$$y_1(t) = \begin{cases} (1 - \tau_1)w(t), & \text{for } t \in [0, t_R], \\ b_1, & \text{for } t \in [t_R, T], \end{cases}$$

$$y_2(t) = \begin{cases} (1 - \tau_2)w(t), & \text{for } t \in [0, t_R], \\ b_2, & \text{for } t \in [t_R, T], \end{cases}$$

$$k(0) = 0, \ k(T) = 0,$$

 $t_1$  random with density  $\phi(t_1)$  and sample space  $[0,\infty]$ .

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Solve recursively.

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Solve recursively. **Step 1**: for  $t \in [t_1, T]$ ,

$$c_{2}^{*}(t|t_{1},k(t_{1})) = \frac{k(t_{1}) + \int_{t_{1}}^{T} e^{-r(v-t_{1})} y_{2}(v) dv}{\int_{t_{1}}^{T} e^{-r(v-t_{1}) + (r-\rho)v/\sigma} \Psi(v)^{1/\sigma} dv} e^{(r-\rho)t/\sigma} \Psi(t)^{1/\sigma}.$$

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$$c_{2}^{*}(t|t_{1},k(t_{1})) = \frac{k(t_{1}) + \int_{t_{1}}^{T} e^{-r(v-t_{1})} y_{2}(v) dv}{\int_{t_{1}}^{T} e^{-r(v-t_{1}) + (r-\rho)v/\sigma} \Psi(v)^{1/\sigma} dv} e^{(r-\rho)t/\sigma} \Psi(t)^{1/\sigma}$$

**Step 2**: Using this and working backwards, the pre-reform solution  $(c_1^*(t), k_1^*(t))_{t \in [0,T]}$  solves (guess and iterate on c(0)):

$$\frac{dc(t)}{dt} = \left(\frac{c(t)^{\sigma}}{\Psi(t)} \left[\frac{k(t) + \int_{t}^{T} e^{-r(v-t)} y_{2}(v) dv}{\int_{t}^{T} e^{-r(v-t) + (r-\rho)v/\sigma} \Psi(v)^{1/\sigma} dv}\right]^{-\sigma} e^{(\rho-r)t} - 1\right) \\
\times c(t) \left[\frac{\sigma}{\phi(t)} \int_{t}^{\infty} \phi(t_{1}) dt_{1}\right]^{-1} + \left[\frac{d\Psi(t)}{dt} \frac{1}{\Psi(t)} + r - \rho\right] \frac{c(t)}{\sigma}, \\
\frac{dk(t)}{dt} = rk(t) + y_{1}(t) - c(t), \\
k(0) = 0, \ k(T) = 0.$$

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## Welfare cost

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## Welfare cost

Consider a no-risk world where  $c^{NR}(t)$  is the solution to

$$\begin{aligned} \max_{c(t)_{t\in[0,T]}} &: \int_0^T e^{-\rho t} \Psi(t) u(c(t)) dt, \text{ subject to,} \\ & dk(t)/dt = rk(t) - c(t), \\ k(0) &= \int_0^T \phi(t_1) Y(t_1) dt_1 + \left[ \int_T^\infty \phi(t_1) dt_1 \right] \int_0^T e^{-rv} y_1(v) dv, \, k(T) = 0, \\ & Y(t_1) \equiv \int_0^{t_1} e^{-rv} y_1(v) dv + \int_{t_1}^T e^{-rv} y_2(v) dv. \end{aligned}$$

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$$\int_{0}^{T} \phi(t_{1}) \left( \int_{0}^{t_{1}} e^{-\rho t} \Psi(t) u[c_{1}^{*}(t)] dt + \int_{t_{1}}^{T} e^{-\rho t} \Psi(t) u[c_{2}^{*}(t|\cdot)] dt \right) dt_{1} \\ + \left[ \int_{T}^{\infty} \phi(t_{1}) dt_{1} \right] \int_{0}^{T} e^{-\rho t} \Psi(t) u[c_{1}^{*}(t)] dt.$$

## Parameterization

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## Parameterization

• Survival data from SSA's cohort mortality tables, which reflect intermediate projections in the 2013 Trustees Report (male cohort born in 1990—turn 25 and enter labor market in 2015).

• CRRA  $u(c(t)) = c(t)^{1-\sigma}/(1-\sigma)$  with  $\sigma = 3$ , and discount rate  $\rho = 0$ .

• Life-cycle wages: Gourinchas and Parker (2002, Econometrica). Fit a 5th-order polynomial.

• Interest rate r = 2.9% (long-run real interest rate assumed in the 2013 Trustees Report).

• We assume that reform is a Weibull random variable,

$$\phi(t_1) = \frac{\mu}{\gamma} \left(\frac{t_1}{\gamma}\right)^{\mu-1} e^{-(t_1/\gamma)^{\mu}}, \text{ for } t_1 \in [0,\infty].$$

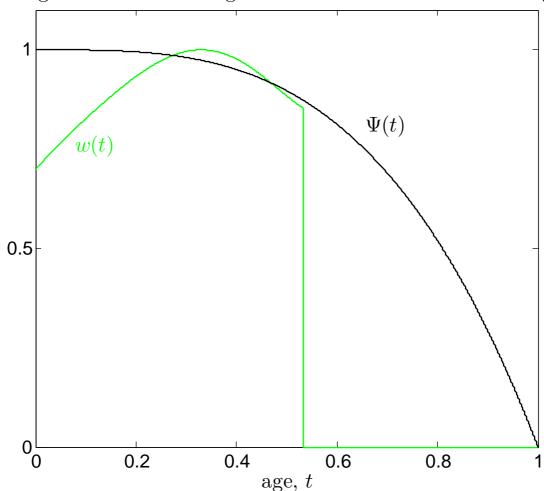


Figure 1. Baseline Wage Profile and Survival Uncertainty

Survival data: SSA 1990 cohort. Wage data: Gourinchas and Parker (2002).

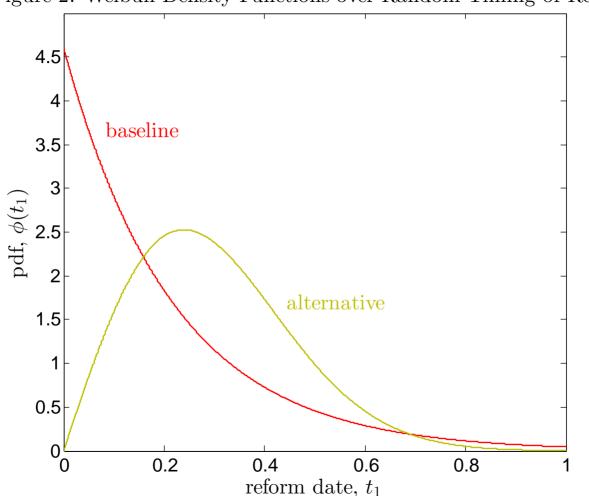


Figure 2. Weibull Density Functions over Random Timing of Reform

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income class	income	replacement rate (if claimed at 65)
very low	$0.25\bar{w}$	67.5%
low	$0.45\bar{w}$	49.0%
average	$\bar{w}$	36.4%
high	$1.6\bar{w}$	30.1%
max		24.0%

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$\max$		24.0%

• Full benefit cut: across-the-board reduction for all current and future retirees,  $(\tau_2, b_2) = (\tau_1, b_1 \times (1 - 21\%))$ .

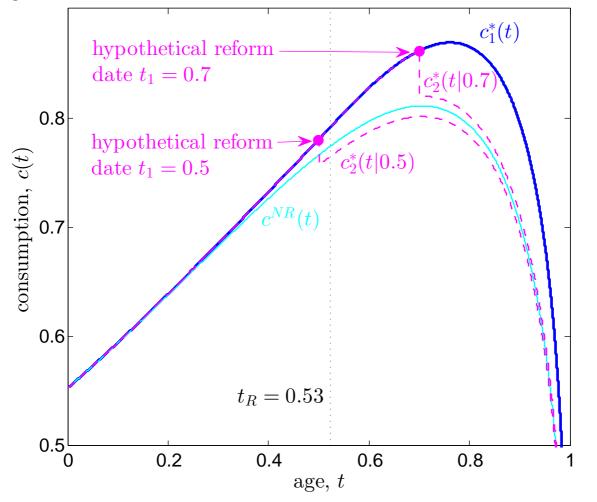
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• Full benefit cut: across-the-board reduction for all current and future retirees,  $(\tau_2, b_2) = (\tau_1, b_1 \times (1 - 21\%))$ .

• Full tax increase: across-the-board increase for all taxpayers,  $(\tau_2, b_2) = (\tau_1 + 3.1\%, b_1)$ .

Figure 3. The Case of **Benefit Reform** with Stochastic Reform Date



Social security parameters:  $\tau_1 = 0.106$ ,  $\tau_2 = 0.106$ ,  $b_1 = 0.322$ ,  $b_2 = 0.254$ .

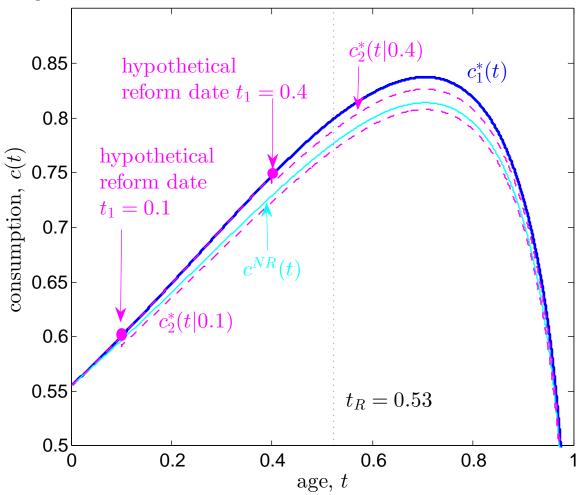


Figure 4. The Case of **Tax Reform** with Stochastic Reform Date

Social security parameters:  $\tau_1 = 0.106$ ,  $\tau_2 = 0.137$ ,  $b_1 = 0.322$ ,  $b_2 = 0.322$ .

## Welfare calculations

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• For an average earner with constant hazard rate of reform, the welfare loss from uncertainty about the timing of benefit reform is 0.01% of lifetime consumption.

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Table 1. Welfare Loss from Timing Uncertainty:

	Full Benefit Reform	Full Tax Reform
Income Level	(21% benefit cut)	(3.1  ppt increase)
very low	2.39	1.70
low	1.51	1.91
average	1.00*	2.07
high	0.78	2.16
max	0.60	2.25

#### Table 1. Welfare Loss from Timing Uncertainty:

Panel B. Alternative Density with Mode at 2033

	Full Benefit Reform	Full Tax Reform
Income Level	(21% benefit cut)	(3.1  ppt increase)
very low	1.04	1.35
low	0.75	1.52
average	0.58	1.66
high	0.51	1.74
max	0.46	1.81

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• Households don't know timing or structure of reform.

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- Households don't know timing or structure of reform.
- New policy depends on random variable  $\alpha$ :

$$\begin{aligned} \tau_2(\alpha) &= \tau_1 + \alpha (\tilde{\tau}_2 - \tau_1), \\ b_2(\alpha) &= b_1 - (1 - \alpha) (b_1 - \tilde{b}_2). \end{aligned}$$

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After solving for  $c^{NR}$  and  $c_1^*$  and  $c_2^*$ , compute  $\Delta$ 

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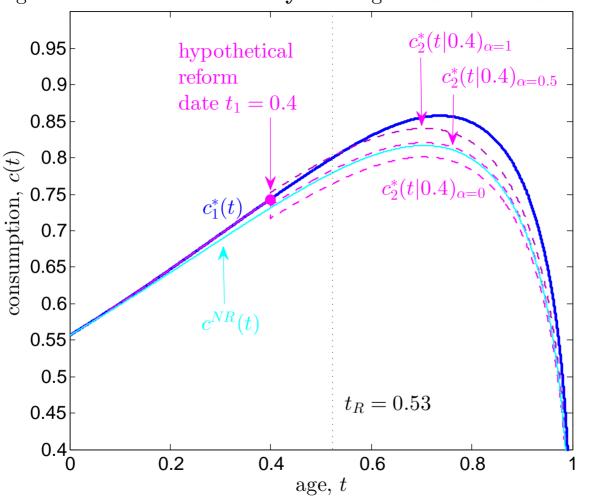
After solving for  $c^{NR}$  and  $c_1^*$  and  $c_2^*$ , compute  $\Delta$ 

$$\int_{0}^{T} D(t)u[c^{NR}(t)(1-\Delta)]dt$$

$$= \int_{0}^{1} \int_{0}^{T} \theta(\alpha)\phi(t_{1}) \left(\int_{0}^{t_{1}} D(t)u[c_{1}^{*}(t)]dt + \int_{t_{1}}^{T} D(t)u[c_{2}^{*}(t|\cdot)]dt\right) dt_{1}d\alpha$$

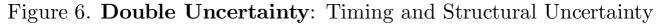
$$+ \left[\int_{T}^{\infty} \phi(t_{1})dt_{1}\right] \int_{0}^{T} e^{-\rho t}\Psi(t)u[c_{1}^{*}(t)]dt.$$
where  $D(t) \equiv e^{-\rho t}\Psi(t)$ .

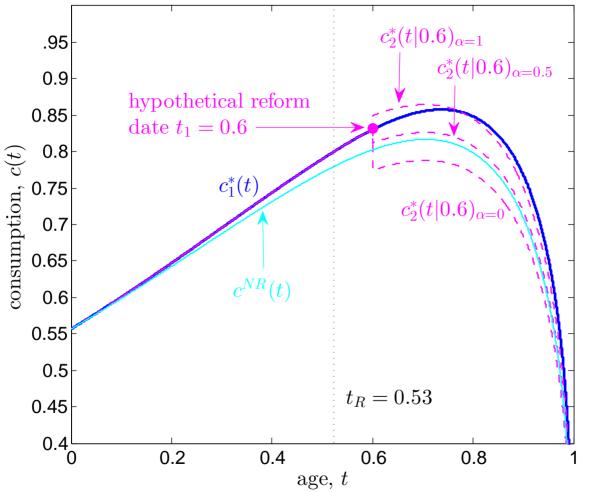
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The share of the budget crisis resolved through extra taxation is  $\alpha$ , and the share resolved through benefit adjustments is  $1 - \alpha$ .







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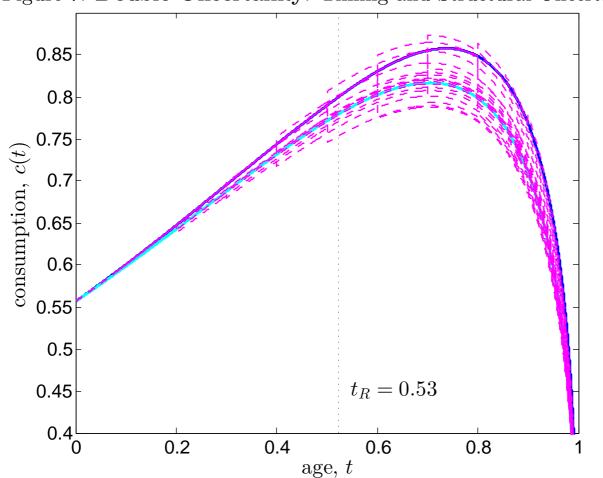


Figure 7. Double Uncertainty: Timing and Structural Uncertainty

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• Let  $\theta(\alpha)$  be uniform.

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• Let  $\theta(\alpha)$  be uniform.

#### Table 2. Welfare Loss: Timing & Structural Uncertainty

Panel A. Co	onstant Hazard	Rate	of Reform
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	Benefit Reform	Tax Reform	Double
Income	(21% benefit cut)	(3.1  ppt increase)	Uncertainty
very low	2.39	1.70	3.09
low	1.51	1.91	1.96
average	1.00*	2.07	1.45
high	0.78	2.16	1.27
max	0.60	2.25	1.19

#### Table 2. Welfare Loss: Timing & Structural Uncertainty

Panel B.	Alternative	Density	with	Mode	at	2033
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	Benefit Reform	Full Tax Reform	Double
Income	(21% benefit cut)	(3.1  ppt increase)	Uncertainty
very low	1.04	1.35	3.60
low	0.75	1.52	2.17
average	0.58	1.66	1.47
$\operatorname{high}$	0.51	1.74	1.22
$\max$	0.46	1.81	1.06

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• Preference parameters: welfare costs  $\uparrow$  when  $\uparrow \sigma$  or  $\uparrow \rho$ .

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- Uniform reform dates: welfare costs  $\uparrow$  and regressivity  $\uparrow$  when reform shock is distributed uniformly over lifetime.

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- Preference parameters: welfare costs  $\uparrow$  when  $\uparrow \sigma$  or  $\uparrow \rho$ .
- Uniform reform dates: welfare costs  $\uparrow$  and regressivity  $\uparrow$  when reform shock is distributed uniformly over lifetime.
- Extreme political risks: welfare costs  $\uparrow$  and regressivity  $\uparrow$  when either D's or R's win the tug-of-war with no chance for compromise.

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- Preference parameters: welfare costs  $\uparrow$  when  $\uparrow \sigma$  or  $\uparrow \rho$ .
- Uniform reform dates: welfare costs  $\uparrow$  and regressivity  $\uparrow$  when reform shock is distributed uniformly over lifetime.
- Extreme political risks: welfare costs  $\uparrow$  and regressivity  $\uparrow$  when either D's or R's win the tug-of-war with no chance for compromise.
- Differential mortality: welfare costs essentially same under differential mortality by income type.

• Methodology to study how timing and structural uncertainty jointly affect economic decision making and welfare.

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• Micro welfare effects of uncertainty over the timing and structure of SS reform.

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• Methodology to study how timing and structural uncertainty jointly affect economic decision making and welfare.

• Micro welfare effects of uncertainty over the timing and structure of SS reform.

• Consistent theme: reform uncertainty hits low-income groups especially hard.

• All of the costs that we report in this paper disappear if gov't simply announces when and how SS will be reformed.