## Happy Together: A Structural Model of Couples' Joint Retirement Choices

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## Introduction

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Main contribution of the paper is analysis of retirement at the couple level.

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- Income
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This paper aims to bridge the gap between the two strands

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- Retirement is not an absorbing state
- Benefit receipt is an absorbing state


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z_{t}=\left\{A_{t}, E_{t}^{m}, E_{t}^{f}, w_{t}^{m}, w_{t}^{f}, B_{t}^{m}, B_{t}^{f}, \text { agediff }\right\}
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Unobservable variables

$$
\varepsilon_{t}=\left\{\varepsilon_{t}\left(d_{t}\right) \mid d_{t} \in D\right\}
$$

## Model

## PREFERENCES

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Household utility

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Household utility

$$
U\left(d_{t}, s_{t} ; z_{t}, \varepsilon_{t}, \theta_{1}\right)=\phi U^{m}\left(c_{t}, l_{t}^{m}\right)+(1-\phi) U^{f}\left(c_{t}, l_{t}^{f}\right)+\varepsilon_{t}\left(d_{t}\right)
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U^{j}=\frac{1}{1-\rho}\left(c_{t}^{\alpha_{1}^{j}}\left(\nu_{t}^{j}\right)^{1-\alpha_{1}^{j}}\right)^{1-\rho}
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U^{j}=\frac{1}{1-\rho}\left(c_{t}^{\alpha_{1}^{j}}\left(\nu_{t}^{j}\right)^{1-\alpha_{1}^{j}}\right)^{1-\rho} \\
\nu_{t}^{j}=L-h_{t}^{j}\left(d_{t}^{j}\right)+\alpha_{2} I\left(d_{t}^{m}=R, d_{t}^{f}=R\right)
\end{gathered}
$$

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## BUDGET CONSTRAINT

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$$
c_{t}+s_{t}=A_{t}+Y\left(r A_{t}, w_{t}^{m} h_{t}^{m}, w_{t}^{f} h_{t}^{f}, \tau\right)+B_{t}^{m} \times s s b_{t}^{m}+B_{t}^{f} \times s s b_{t}^{f}+T_{t}
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Liquidity constraint:

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Liquidity constraint:

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s_{t} \geq 0
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- Workers retiring at 62 receive $80 \%$ of PIA


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- Benefits are indexed to CPI
- Earnings test


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- Earnings test
- Dependent spouse benefit


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- Workers retiring after 65 receive $5.5 \%$ increase per year
- Benefits are indexed to CPI
- Earnings test
- Dependent spouse benefit
- Surviving spouse benefit


## Model

## STOCHASTIC PROCESSES

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Wage:

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Wage:

$$
\ln w_{i t}=W\left(a g e_{i t}\right)+\varsigma l\left\{d_{i t}=P T\right\}+v_{i t}
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Wage:

$$
\begin{aligned}
& \quad \ln w_{i t}=W\left(\text { age }_{i t}\right)+\varsigma l\left\{d_{i t}=P T\right\}+v_{i t} \\
& v_{i t}=v_{i t-1} \\
& +\xi_{i t}
\end{aligned}
$$

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v_{i t}=v_{i t-1}-\delta_{R} I\left(d_{i t-1}=R\right)-\delta_{P T} I\left(d_{i t-1}=P T\right)+\xi_{i t}
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## STOCHASTIC PROCESSES (contd.)

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E\left(h c_{t} \mid a g e_{t}^{m}, a g e_{t}^{f}\right)=E\left(h c_{t} \mid a g e_{t}^{m}, a g e_{t}^{f}, h c>0\right) P\left(h c t>0 \mid a g e_{t}^{m}, a g e_{t}^{f}\right)
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\ln h c_{t}=h\left(a g e_{t}^{m}, a g e_{t}^{f}\right)+\psi_{t},
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Survival:

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Survival:

$$
s_{t+1}^{j}=s\left(a g e_{t}^{j}\right)
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## Model Solution

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- Framework introduced by Rust $(1987,1988)$ for the solution and estimation of stochastic Markov discrete processes.


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- Framework introduced by Rust $(1987,1988)$ for the solution and estimation of stochastic Markov discrete processes.
- Extend framework in order to account for continuous decisions.


## Model Solution

Households choose a series of decision rules $\Pi=\left\{\pi_{0}, \pi_{1}, \ldots, \pi_{T}\right\}$, where $\pi_{t}\left(z_{t}, \varepsilon_{t}\right)=\left(d_{t}, s_{t}\right)$, to maximize:

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E_{t}\left\{\sum_{i=t}^{T} \beta^{i-t} S_{i-t} U_{t}\left(\theta_{1}\right)\right\}
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The expectation is taken with respect to the controlled stochastic process $\left\{z_{t}, \varepsilon_{t}\right\}$ with probability distribution:

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f\left(z_{t+1}, \varepsilon_{t+1} \mid d_{t}, s_{t}, z_{t}, \varepsilon_{t}, \theta_{2}, \theta_{3}\right)=
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$$
\begin{aligned}
& f\left(z_{t+1}, \varepsilon_{t+1} \mid d_{t}, s_{t}, z_{t}, \varepsilon_{t}, \theta_{2}, \theta_{3}\right)= \\
& q\left(\varepsilon_{t+1} \mid z_{t+1}, \theta_{2}\right) g\left(z_{t+1} \mid z_{t}, d_{t}, s_{t}, \theta_{3}\right)
\end{aligned}
$$

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V_{t}\left(z_{t}, \varepsilon_{t}, \theta\right)=\max _{d_{t}}\left\{\max _{s_{t}}\left\{u\left(k, s_{t}, z_{t}, \theta_{1}\right)+\beta E_{t} V_{t+1}\left(z_{t+1}, k, s_{t}, \theta\right) \mid d_{t}=k\right\}+\varepsilon_{t}\right\}
$$

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V_{t}\left(z_{t}, \varepsilon_{t}, \theta\right)=\max _{d_{t}}\left\{\max _{s_{t}}\left\{u\left(k, s_{t}, z_{t}, \theta_{1}\right)+\beta E_{t} V_{t+1}\left(z_{t+1}, k, s_{t}, \theta\right) \mid d_{t}=k\right\}+\varepsilon_{t}\right\}
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P\left(k \mid z_{t}, \theta\right)=\frac{\exp \left\{r\left(z_{t}, k, \theta\right)\right\}}{\sum_{k \in D} \exp \left\{r\left(z_{t}, k, \theta\right)\right\}}
$$

$>$ graph

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Estimate $\theta_{1}$ using method of simulated moments.

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- Panel data on households where at least one member is aged 51 to 61 in initial wave.
- Extensive information on:
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- Retirement
- Demographics
- HRS data can be linked to Social Security Administration records which provide information on covered earnings and benefits.


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Estimation sample:

- The model is estimated using the sample of HRS couples who do not have a defined benefit pension.
- For individuals with no private pension, Social Security provides main age-specific incentives for retirement.
- The same is true for individuals with defined contribution pensions.
- Defined benefit pensions give very strong incentives for retirement at particular ages, usually different from the Social Security ages.


## Estimation: Second Stage

Table: Preference and Wage Process Parameter Estimates

| Parameter and definition | (1) | (2) |  |
| :--- | :--- | :--- | :--- |
| $\alpha_{1}^{m}$ | Consumption share, male U function | 0.5102 |  |
| $\alpha_{1}^{f}$ | Consumption share, female U function | 0.4295 |  |
| $\alpha_{2}$ | Value of shared retirement |  |  |
|  | Male's wage depreciation per year PT | 0.9051 |  |
|  | Female's wage depreciation per year PT | 0.8933 |  |
|  | Male's wage depreciation per year R | 0.8092 |  |
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| $\alpha_{2}$ | Value of shared retirement |  | 0.0891 |
|  |  |  | $(0.0079)$ |
|  | Male's wage depreciation per year PT | 0.9051 | 0.9258 |
|  |  |  | $(0.0383)$ |
|  | Female's wage depreciation per year PT | 0.8933 |  |
|  | Male's wage depreciation per year R | 0.8092 |  |
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|  | Female's wage depreciation per year PT | 0.8933 | 0.9219 |
|  |  |  | (0.0334) |
|  | Male's wage depreciation per year R | 0.8092 | 0.8609 |
|  |  |  | (0.0436) |
|  | Female's wage depreciation per year R | 0.7795 | 0.7841 |
|  |  |  | (0.0336) |
| GMM criterion |  | 0.2058 | 0.1404 |

Figure: Simulated vs. actual age profiles for total participation, men.


Figure: Simulated vs. actual age profiles for total participation, women.


Figure: Simulated vs. actual age profiles for FT/PT participation, men.


Figure: Simulated vs. actual age profiles for FT/PT participation, women.


Figure: Simulated vs. actual retirement frequencies, men.


Figure: Simulated vs. actual retirement frequencies, women.


Figure: Simulated vs. actual joint retirement frequencies.


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- Results show that positive complementarity parameters explain $8 \%$ of joint retirements...
- ...while social security's spousal benefit accounts for another $13 \%$.

Figure: Retirement frequencies for married men and women


Figure: Optimal participation choices as a function of $E^{m}, E^{f}$


Figure: Differences in retirement dates by age difference between spouses


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