

# *Optimal Design of Welfare-to-Work Programs*

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# Introduction

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  - ▶ Mandatory Work: “work in exchange for benefits”
  - ▶ Transitional Work: “stepping stone” to private sector job

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  - ▶ Training
  - ▶ Earnings subsidies/employment bonuses

## Language and question

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- A *policy* is a prescription of an activity (search, work, train, or rest) to the participant, with an associated conditional transfer
- A *WTW program* is a government expenditure program that combines different *policies*
- An *optimal WTW program* minimizes government expenditures s.t. delivering a given level of ex-ante utility to the participant



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**Question:** how to optimally design a welfare-to-work (WTW) program

## Approach: dynamic contracting

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- Point of departure: optimal UI literature
  - ▶ Shavell-Weiss (1979): unobservable job search effort
  - ▶ Hopenhayn-Nicolini (1997): recursive formulation

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- Critique
  - ▶ Excessive focus on optimal level and path of UI benefits  
Cahuc-Lehmann (2000), Hassler-Rodriguez Mora (2002), Kocherlakota (2004), Coles-Masters (2007), Pavoni (2007), Chetty (2008), Sanchez (2008), Shimer-Werning (2008), Hagedorn-Kaul-Mennel (2010), Landais-Michaillat-Saez (2010), Michelacci-Ruffo (2011)

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  - ▶ Policy debate is on which instrument is best for whom
- Generalization
  - ▶ additional technologies  $\leftrightarrow$  policies
  - ▶ human capital (agent heterogeneity)

# 1. ECONOMIC ENVIRONMENT

# Preferences, endowments, and storage

---

- Agent is infinitely lived with discount factor  $\beta \in (0, 1)$
- Intra-period utility:  $\log(c) - a$ 
  - ▶ Consumption  $c \geq 0$  and effort  $a \in \{0, e\}$

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- Agent endowed with fixed human capital  $h$
- Storage with return  $R = \beta^{-1}$
- No access to credit

# Rest, search, and private-sector job

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  - ▶ Low effort ( $a = 0$ )
- Job search
  - ▶ Job-finding probability:  $\pi(h) \equiv \pi(h, e) > \pi(h, 0) \equiv 0$
  - ▶ Success of job search  $\rightarrow$  private sector job

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- **Job search**
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  - ▶ Success of job search  $\rightarrow$  private sector job
- **Private-sector job (absorbing state)**
  - ▶ Requires high effort ( $a = e$ ) to produce  $\omega(h) \geq 0$

**Remark:** search effort can be **lower** than work effort

- Krueger-Muller (2010); Aguiar-Hurst-Karabarbounis (2012)

## Additional technologies

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- Search Assistance
  - ▶ At cost  $\kappa^A$ , agency takes over search on behalf of participant
  - ▶ Participant saves her search effort
  - ▶ Agency's search equally efficient as private search

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- **Search Assistance**
  - ▶ At cost  $\kappa^A$ , **agency takes over search** on behalf of participant
  - ▶ Participant saves her search effort
  - ▶ Agency's search equally efficient as private search
- **Public-sector production**
  - ▶ At cost  $\kappa^P$ , **public job** readily available (no search friction)
  - ▶ Requires high effort ( $a = e$ ) to produce  $\underline{\omega} \geq 0$

# Information structure

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- **Observable and contractible:**
  - ▶ Agent type  $h$
  - ▶ Work effort on public & private jobs (e.g., supervised)
  - ▶ Saving ( $= 0$ )

# Information structure

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- **Observable and contractible:**
  - ▶ Agent type  $h$
  - ▶ Work effort on public & private jobs (e.g., supervised)
  - ▶ Saving ( $= 0$ )
- **Private information** of the agent and under her control:
  - ▶ Job-search effort (IC-Search)
  - ▶ Job offer upon contact (IC-Retention)



## 2. CONTRACT

# Principal-Agent relationship

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- Risk neutral principal who discounts at rate  $R^{-1} = \beta$

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- At every pair  $(U, h)$ , the contract specifies:
  - ▶ **Effort level:**  $a \in \{0, e\}$
  - ▶ **Activity:** assignment to technology
  - ▶ **Payments:** welfare benefits/wage tax or subsidy
  - ▶ **Continuation utility:**  $(U^s, U^f)$  conditional on outcome of activity

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# Principal-Agent relationship

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- Risk neutral principal who discounts at rate  $R^{-1} = \beta$
- Recursive formulation with states:  $(U, h)$  and employment status
- At every pair  $(U, h)$ , the **Markovian** contract specifies:
  - ▶ **Effort level**:  $a \in \{0, e\}$
  - ▶ **Activity**: assignment to technology
  - ▶ **Payments**: welfare benefits/wage tax or subsidy
  - ▶ **Continuation utility**: only conditional on employment status

## Options of contract as policies of WTW program

---

- Combination of prescriptions on effort  $a$  and use of technologies leads to **five policy instruments** ( $i$ ):
  - ▶ **SA** : Social Assistance (rest,  $a = 0$ )
  - ▶ **UI** : Unemployment Insurance (private search,  $a = e$ )
  - ▶ **JA** : Job-search Assistance (assisted search,  $a = 0$ )
  - ▶ **MW** : Mandatory Work (public-sector work,  $a = e$ )
  - ▶ **TW** : Transitional Work (public work + assisted search,  $a = e$ )

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$$V(U, h) = \max_{i \in \{SA, UI, JA, MW, TW\}} V^i(U, h)$$



# 3. VALUE FUNCTIONS

## SA and MW

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- Social Assistance (SA)

$$\begin{aligned} V^{SA}(U) &= \max_c -c + \beta V^{SA}(U) \\ \text{s.t.} &: \\ U &= \log(c) + \beta U \quad (PK) \end{aligned}$$

## SA and MW

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- Mandatory Work (MW)

$$\begin{aligned} V^{MW}(U) &= \max_c \underline{\omega} - \kappa^P - c + \beta V^{MW}(U) \\ \text{s.t.} &: \\ U &= \log(c) - e + \beta U \quad (PK) \end{aligned}$$

# Unemployment Insurance (UI)

---

$$V^{UI}(U, h) = \max_{c, U^s} -c + \beta [\pi(h)W(U^s, h) + (1 - \pi(h))V^{UI}(U, h)]$$

**s.t.** :

$$U = \log(c) - e + \beta [\pi(h)U^s + (1 - \pi(h))U] \quad (PK)$$

$$U^s \geq U + \frac{e}{\beta\pi(h)} \quad (IC - S)$$

$$U^s \geq U \quad (IC - R)$$

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## Remark:

- **Job-search Monitoring:** at a cost, eliminate IC-S and IC-R
  - Aiyagari-Alvarez (1995); Pavoni-Violante (2006); Setty (2011)
  - Meyer (1995); van den Berg-van der Klaauw (2006)

## Job-search Assistance (JA)

---

$$V^{JA}(U, h) = \max_{c, U^s} -c - \kappa^A + \beta [\pi(h)W(U^s, h) + (1 - \pi(h))V^{JA}(U, h)]$$

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$$U^s \geq U \quad (IC - R)$$

No search effort → no IC-S

# Transitional Work (TW)

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- Policy combining public-sector work and search assistance

$$V^{TW}(U, h) = \max_{c, U^s} \underline{\omega} - \kappa^P - \kappa^A - c + \beta \left[ \pi(h)W(U^s, h) + (1 - \pi(h))V^{TW}(U, h) \right]$$

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s.t. :

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**IC-R not binding:** both TW and private employment require effort

## Closed-form of value functions

---

$$V^i(U, h) = \frac{1}{1 - \beta} \cdot [A^i(h) - B^i(h) \cdot \exp((1 - \beta)U)]$$

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$$V^i(U, h) = \frac{1}{1 - \beta} \cdot [A^i(h) - B^i(h) \cdot \exp((1 - \beta)U)]$$

- $A^i(h)$ : output net of administrative cost ( $\kappa^A, \kappa^P$ )
- $B^i(h)$ : cost of promising a unit of  $U$  in  $c$  terms (relative to  $SA$ )

# Returns and costs of each policy

---

$$V^i(U, h) = \frac{1}{1 - \beta} \cdot [A^i(h) - B^i(h) \cdot \exp((1 - \beta)U)]$$

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$A^i(h)$ : Net Return

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$B^i(h)$ : Cost of Promising  $U$

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$SA :$   $0$

$MW :$   $\underline{\omega} - \kappa^P$

$UI :$   $\frac{\beta\pi(h)}{1 - \beta + \beta\pi(h)} \omega(h)$

$JA :$   $\frac{\beta\pi(h)}{1 - \beta + \beta\pi(h)} \omega(h) - \frac{1 - \beta}{\beta\pi(h)} \kappa^A$

$TW :$   $\frac{\beta\pi(h)}{1 - \beta + \beta\pi(h)} \omega(h) + \frac{1 - \beta}{\beta\pi(h)} (\underline{\omega} - \kappa^P - \kappa^A)$

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# Returns and costs of each policy

$$V^i(U, h) = \frac{1}{1 - \beta} \cdot [A^i(h) - B^i(h) \cdot \exp((1 - \beta)U)]$$

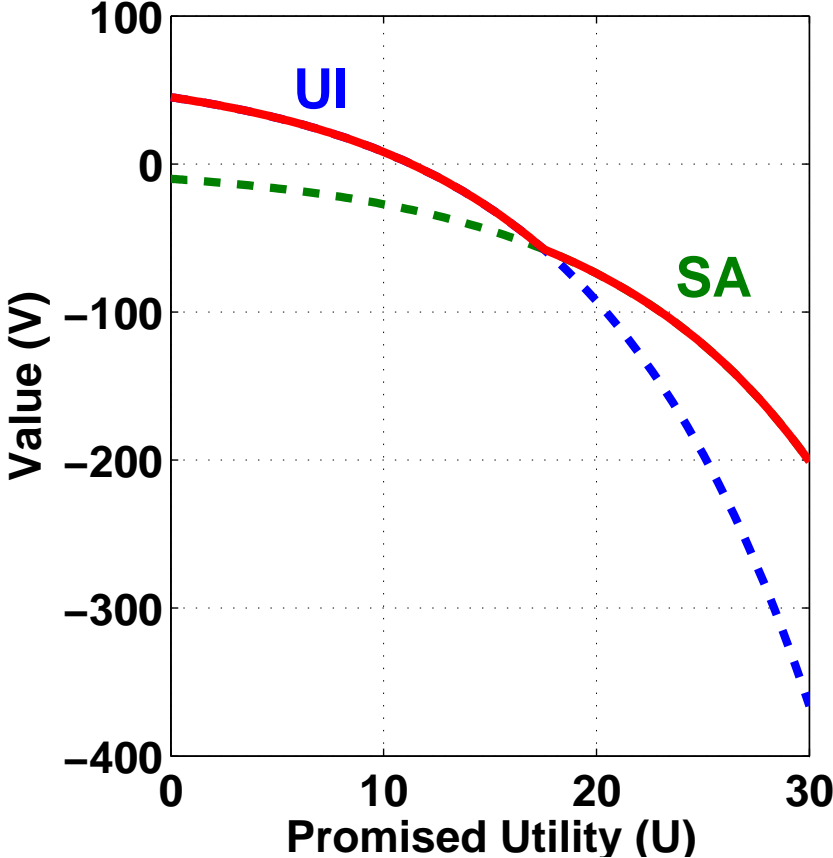
	$A^i(h)$ : Net Return	$B^i(h)$ : Cost of Promising $U$
<i>SA</i> :	0	1
<i>MW</i> :	$\underline{\omega} - \kappa^P$	$\exp(e)$
<i>UI</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)} \omega(h)$	$\frac{1-\beta+\beta\pi(h) \exp\left\{e + \frac{1-\beta}{\beta\pi(h)} e\right\}}{1-\beta+\beta\pi(h)}$
<i>JA</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)} \omega(h) - \frac{1-\beta}{\beta\pi(h)} \kappa^A$	$\frac{1-\beta+\beta\pi(h) \exp(e)}{1-\beta+\beta\pi(h)}$
<i>TW</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)} \omega(h) + \frac{1-\beta}{\beta\pi(h)} (\underline{\omega} - \kappa^P - \kappa^A)$	$\exp(e)$

# Returns and costs of each policy

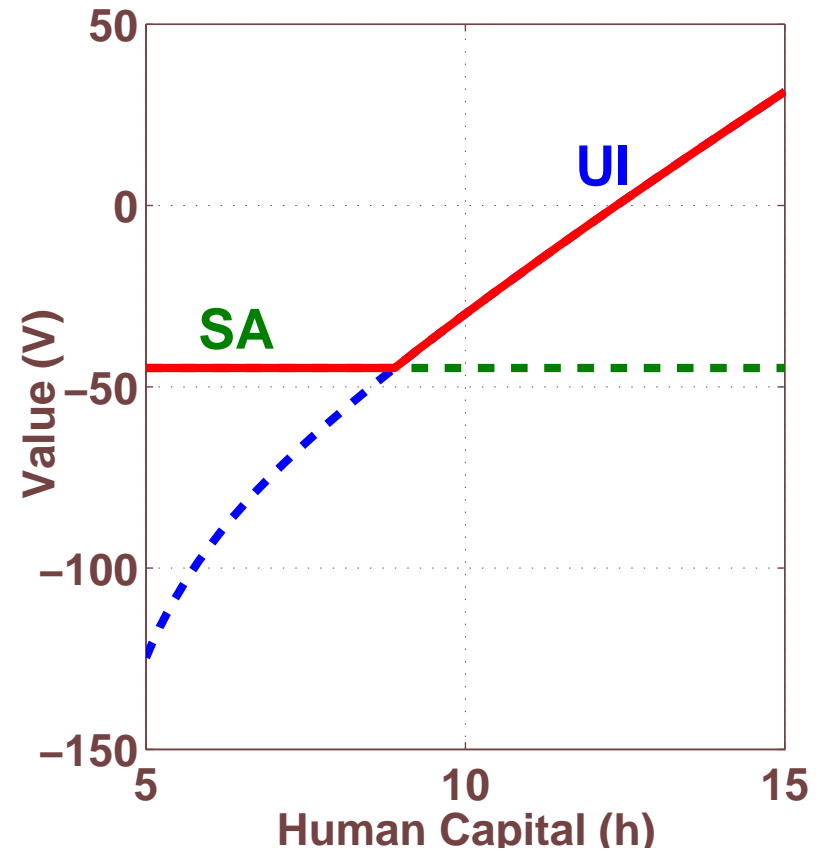
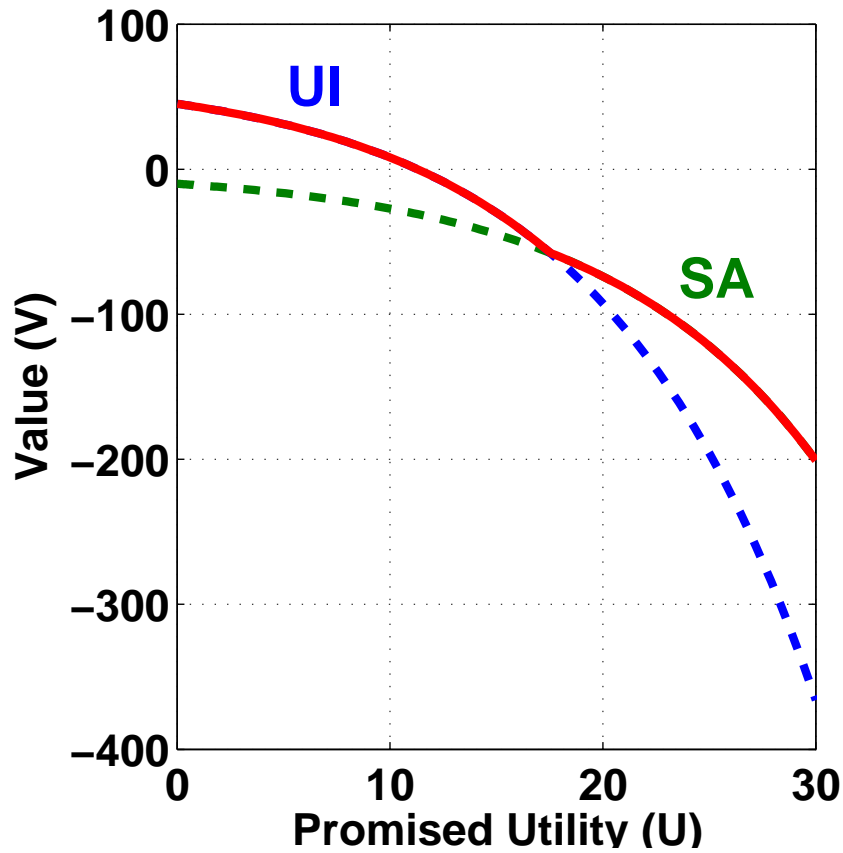
$$V^i(U, h) = \frac{1}{1 - \beta} \cdot [A^i(h) - B^i(h) \cdot \exp((1 - \beta)U)]$$

	$A^i(h)$ : Net Return	$B^i(h)$ : Cost of Promising $U$
<i>SA</i> :	0	1
<i>MW</i> :	$\underline{\omega} - \kappa^P$	$\exp(e)$
<i>UI</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)}\omega(h)$	$\exp(e) \times \text{cost of (IC-S)}$
<i>JA</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)}\omega(h) - \frac{1-\beta}{\beta\pi(h)}\kappa^A$	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)} \exp(e) \times \text{cost of (IC-R)}$
<i>TW</i> :	$\frac{\beta\pi(h)}{1-\beta+\beta\pi(h)}\omega(h) + \frac{1-\beta}{\beta\pi(h)} (\underline{\omega} - \kappa^P - \kappa^A)$	$\exp(e)$

# Value functions: UI - SA comparison



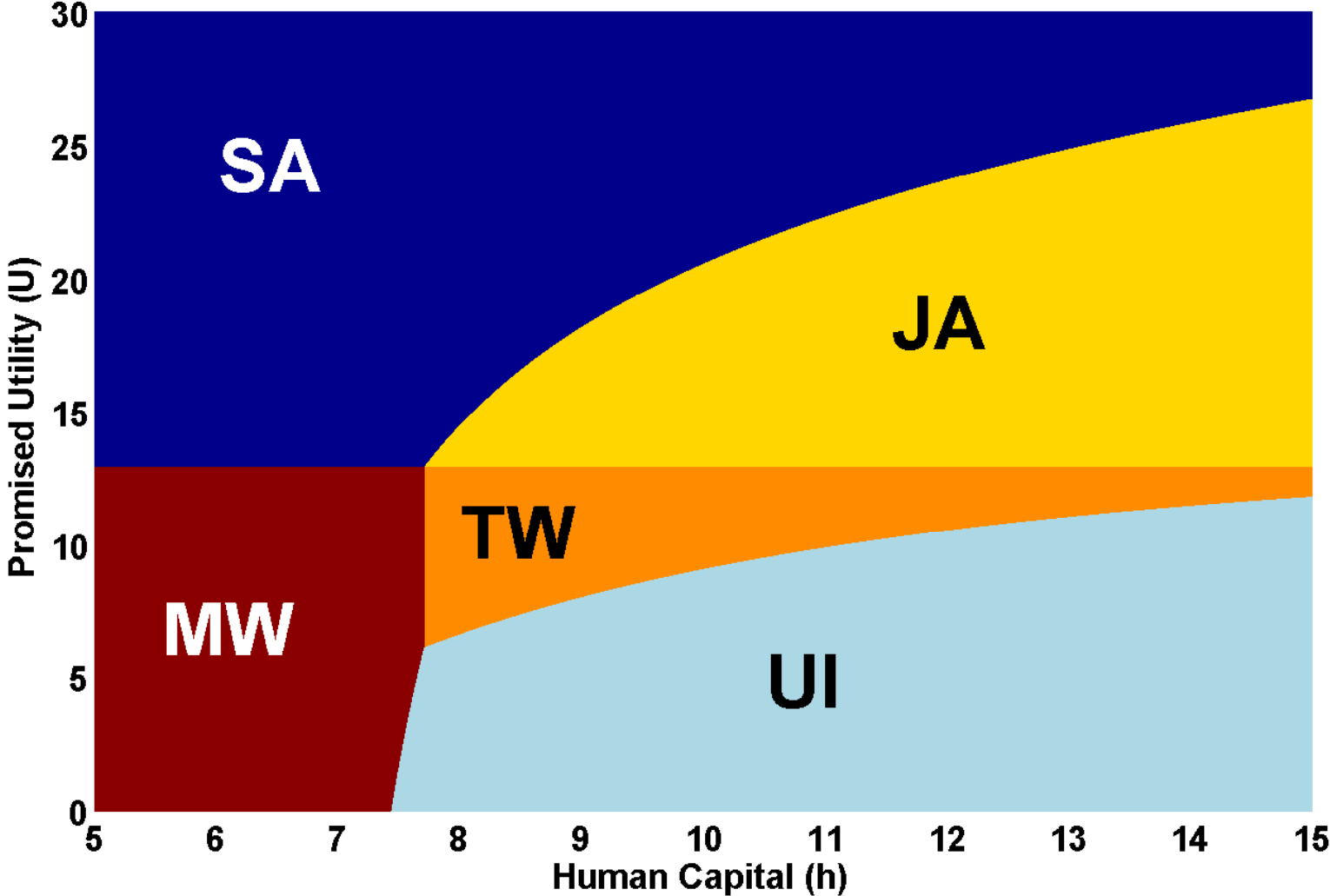
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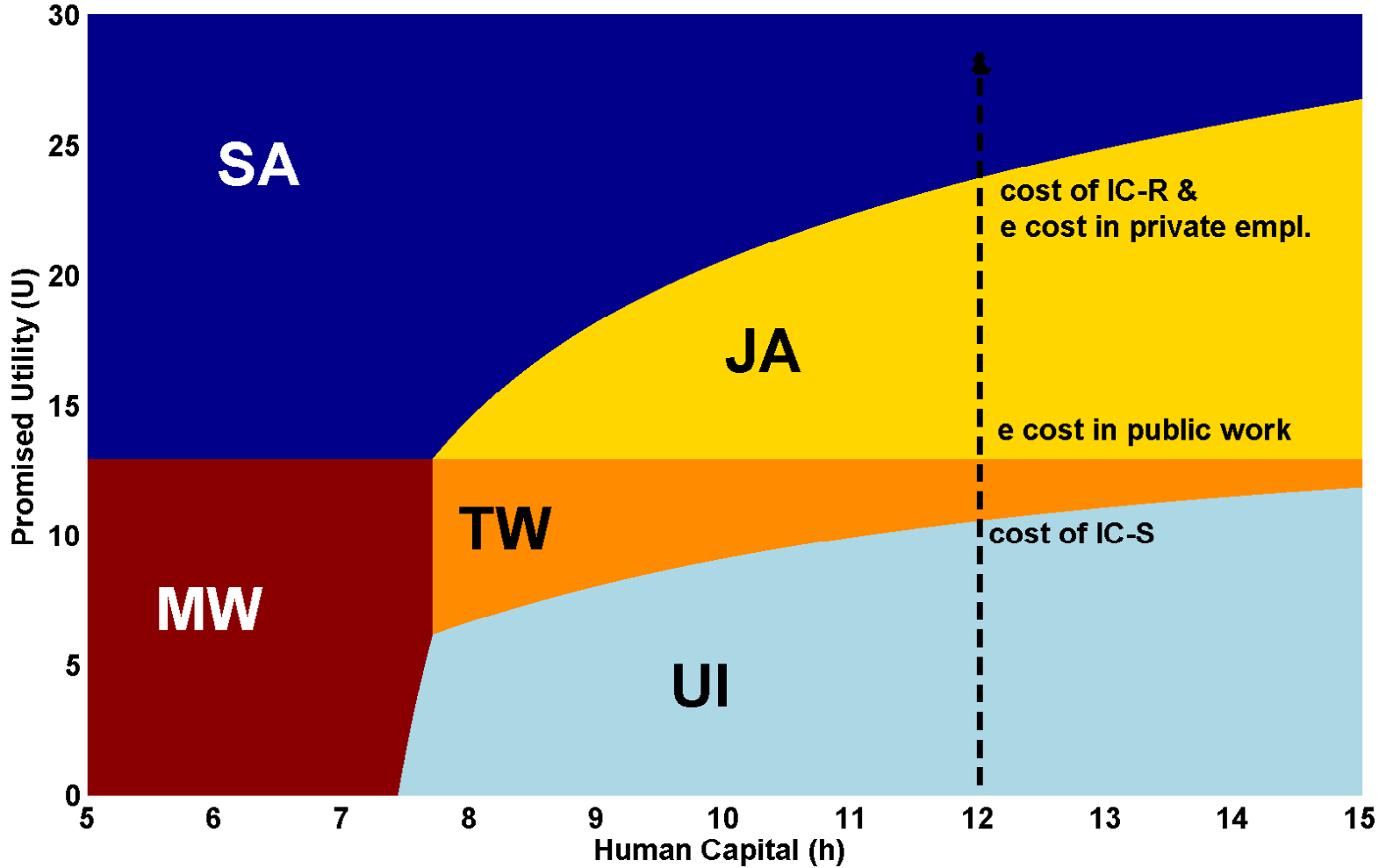


# 4. OPTIMAL WTW PROGRAM

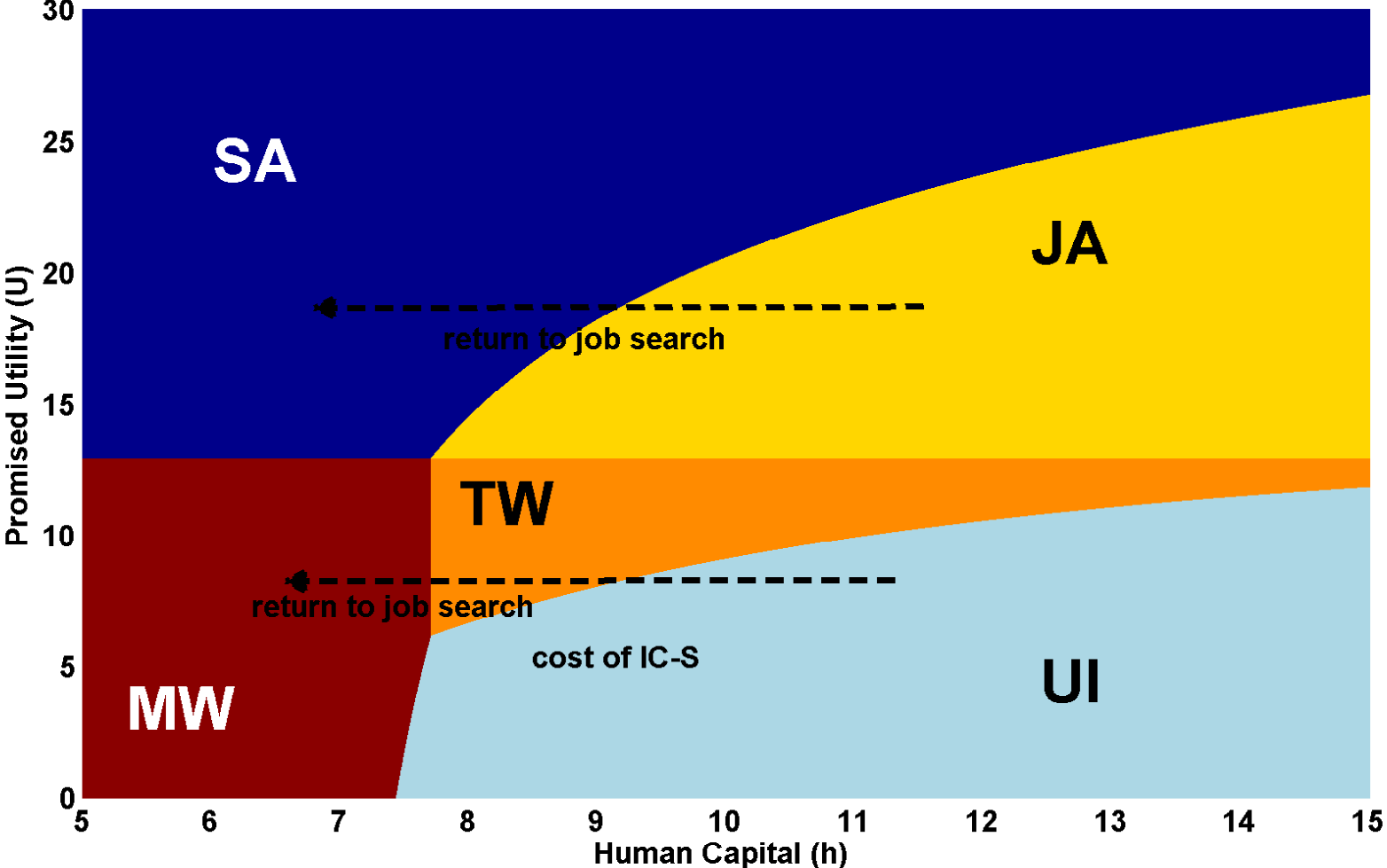
# Optimal WTW program



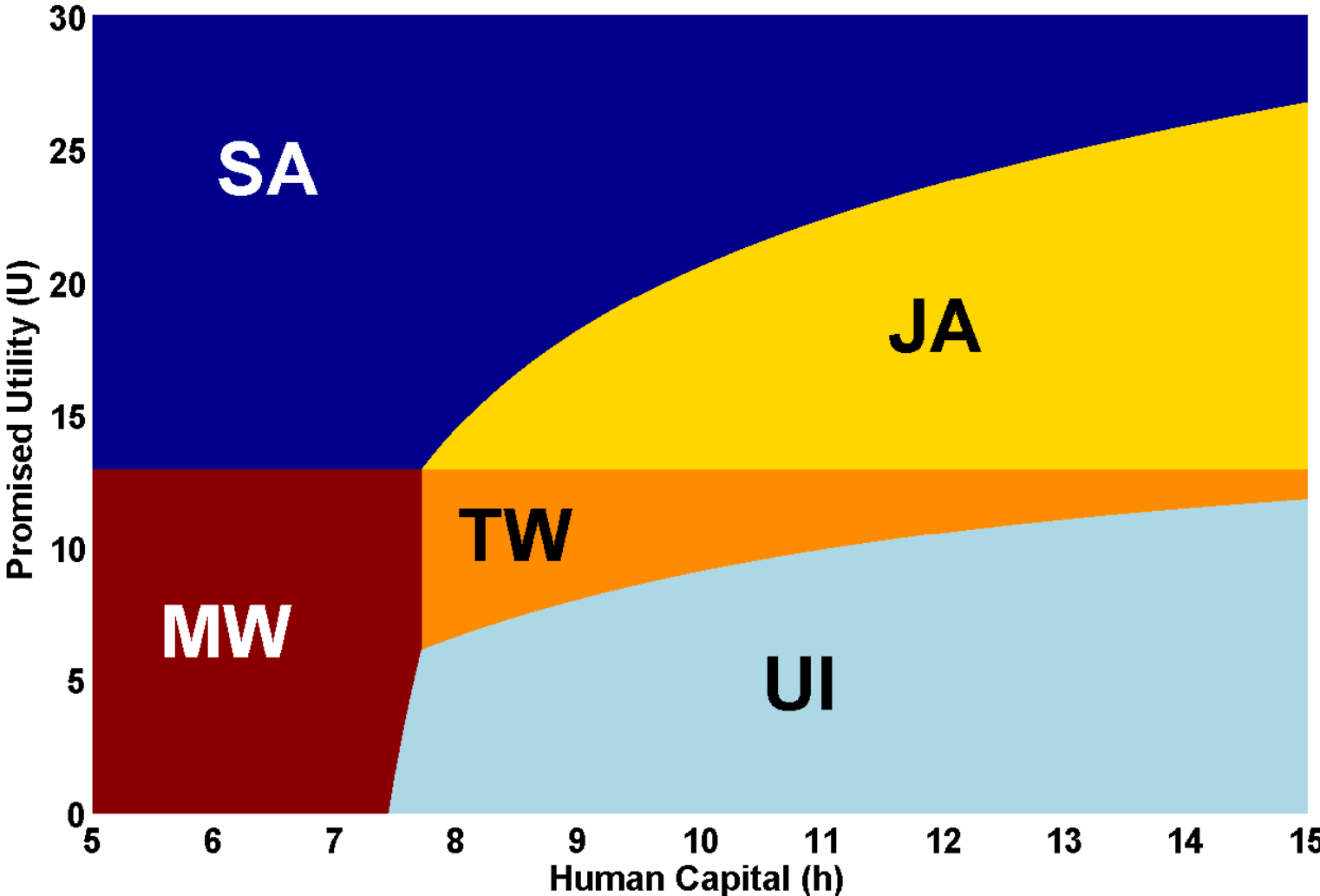
# Comparative statics wrt U



# Comparative statics wrt h



# Optimal WTW program



# 5. HUMAN CAPITAL DYNAMICS

# Human capital depreciation

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Two implications of  $h$  depreciation:

## 1. Skill depreciation ( $\omega$ )

- Jacobson-Lalonde-Sullivan (1993); Kletzer (1998); Couch-Placzek (2010)

- Addison-Portugal (1989); Gregg (2001); Edin-Gustavsson (2008)

## 2. Duration dependence in unemployment ( $\pi$ )

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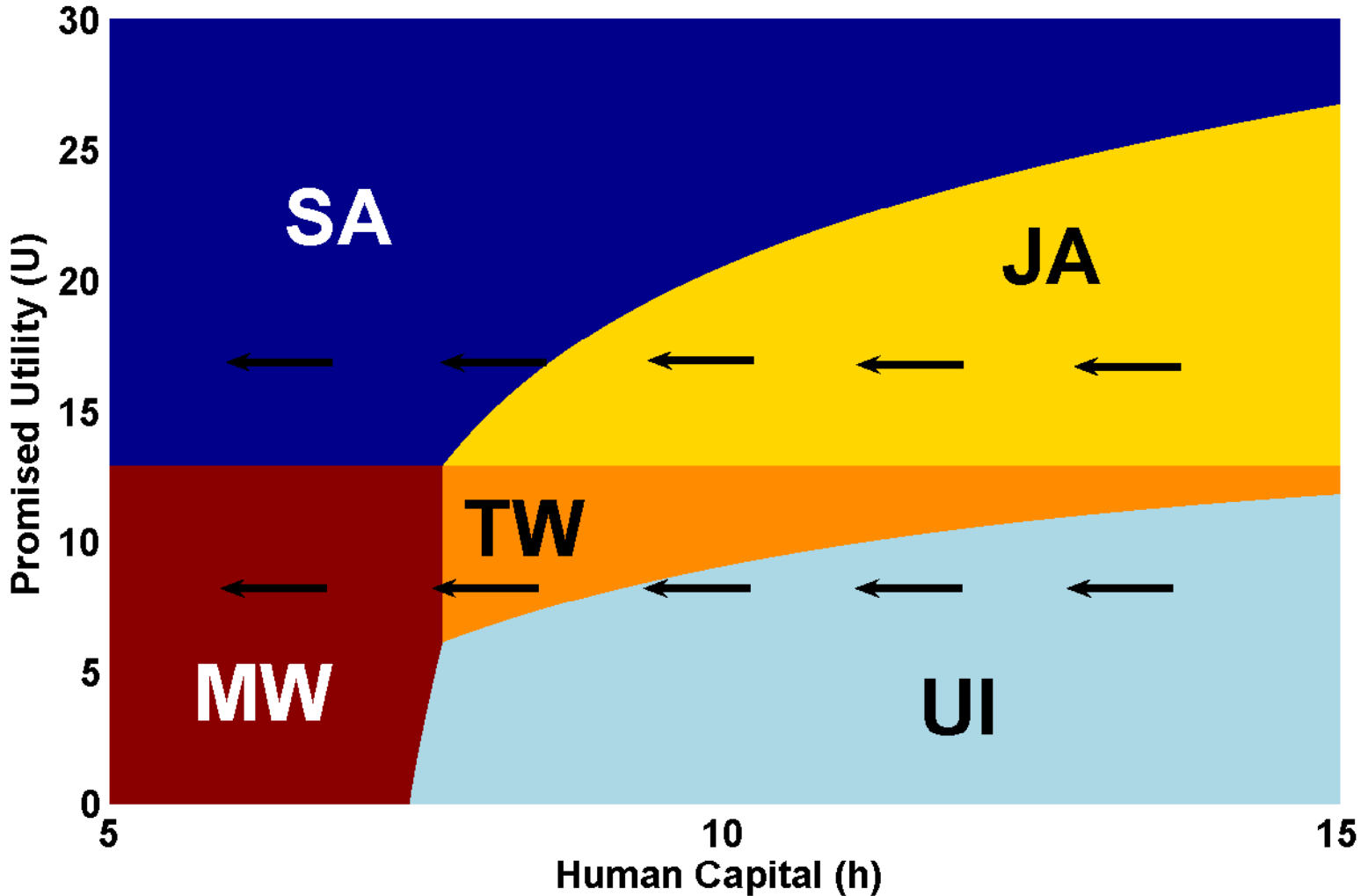
## 2. Duration dependence in unemployment ( $\pi$ )

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New feature of WTW program: **transitions across policies**



# Optimal WTW program



# Summary of optimal policy transitions

---

- Policy transitions induced by  $h$  dynamics
  1. High generosity:  $JA \rightarrow SA$
  2. Low generosity:  $UI \rightarrow TW \rightarrow MW$... and all sub-transitions

# Summary of optimal policy transitions

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- Policy transitions **induced by  $h$  dynamics**
  1. **High generosity:**  $JA \rightarrow SA$
  2. **Low generosity:**  $UI \rightarrow TW \rightarrow MW$... and all sub-transitions
- However, many transitions can be **ruled out as sub-optimal:**
  1. Any transition from  $SA$  or  $MW$
  2. Any transition into  $UI$

# Additional technology: human capital accumulation

---

## Additional technology: human capital accumulation

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- At cost  $\kappa^T$ , the agent is **trained** during the period
- With probability  $\theta$ , training is successful and  $h$  jumps to  $\bar{h}$
- Effort required and **unobservable**

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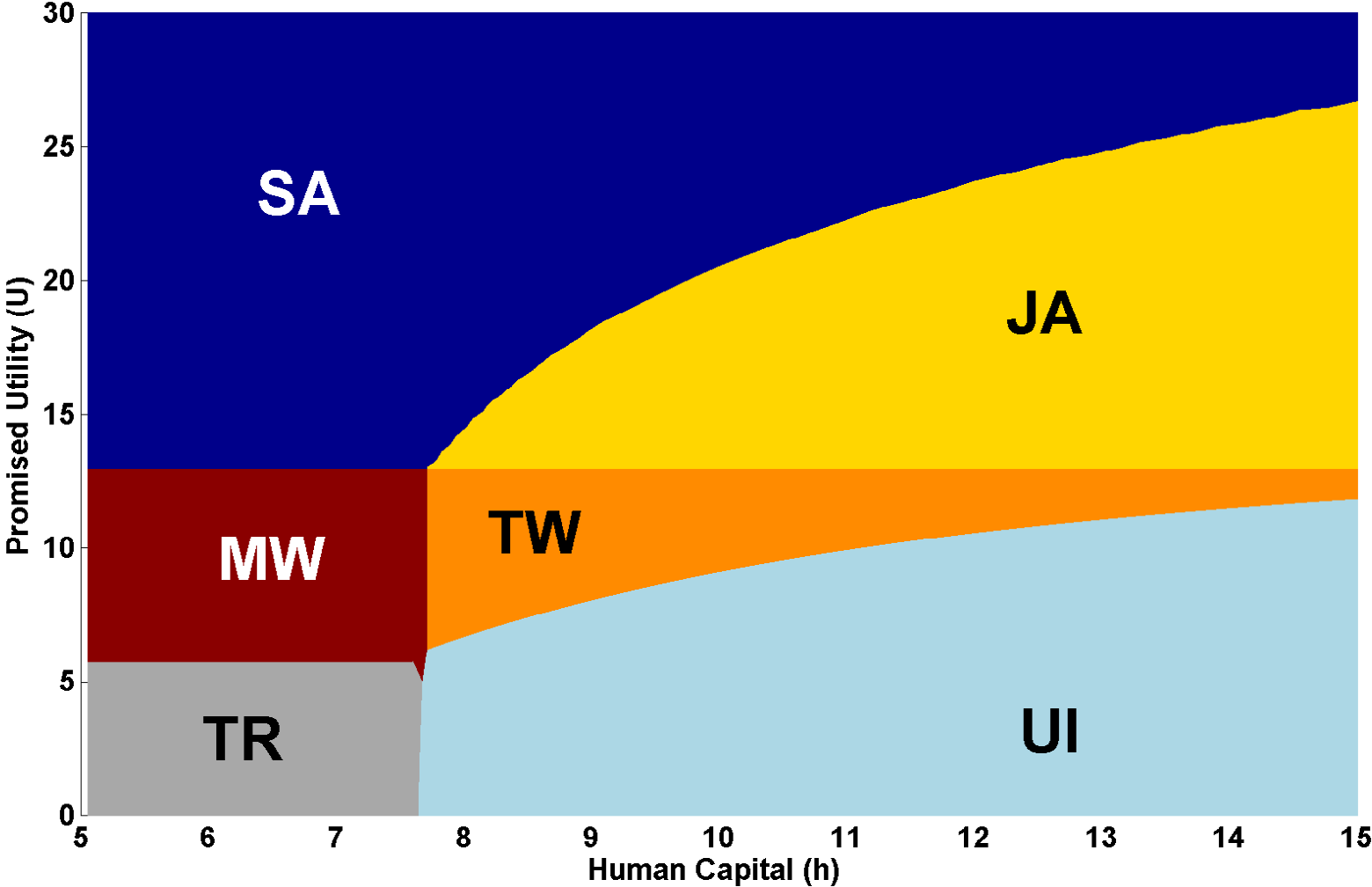
$$V^{TR}(U, h) = \max_{c, U^s} -c - \kappa^T + \beta \{ \theta V(U^s, \bar{h}) + (1 - \theta) \mathbb{E}_h [V(U, h')] \}$$

**s.t.** :

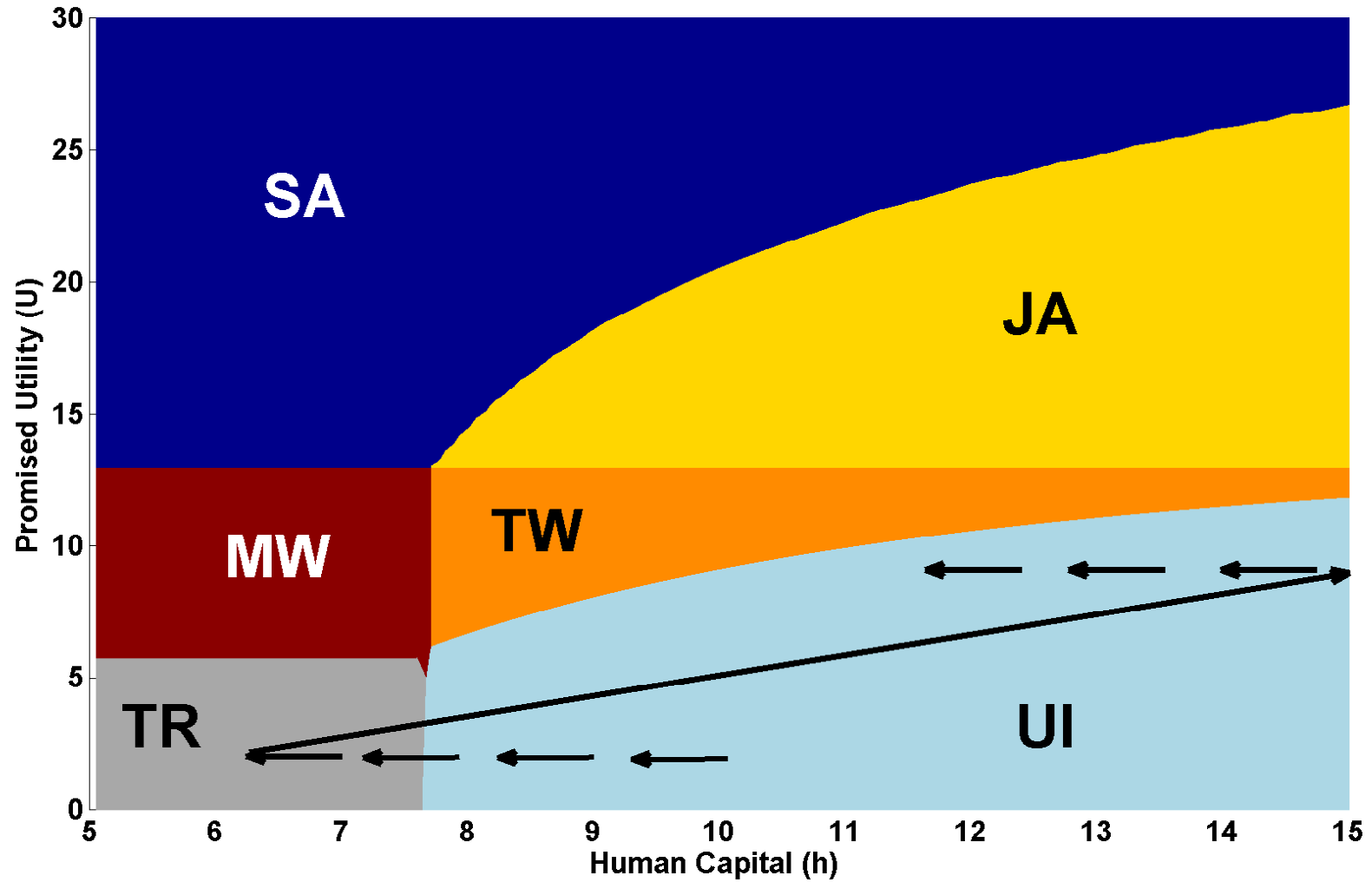
$$U = \log(c) - e + \beta [\theta U^s + (1 - \theta)U] \quad (PK)$$

$$U^s \geq U + \frac{e}{\beta\lambda} \quad (IC - T)$$

# Optimal WTW Program with training



# Policy transitions with training





# 6. DYNAMIC INCENTIVES ( $h$ FIXED)

# Dynamic incentives

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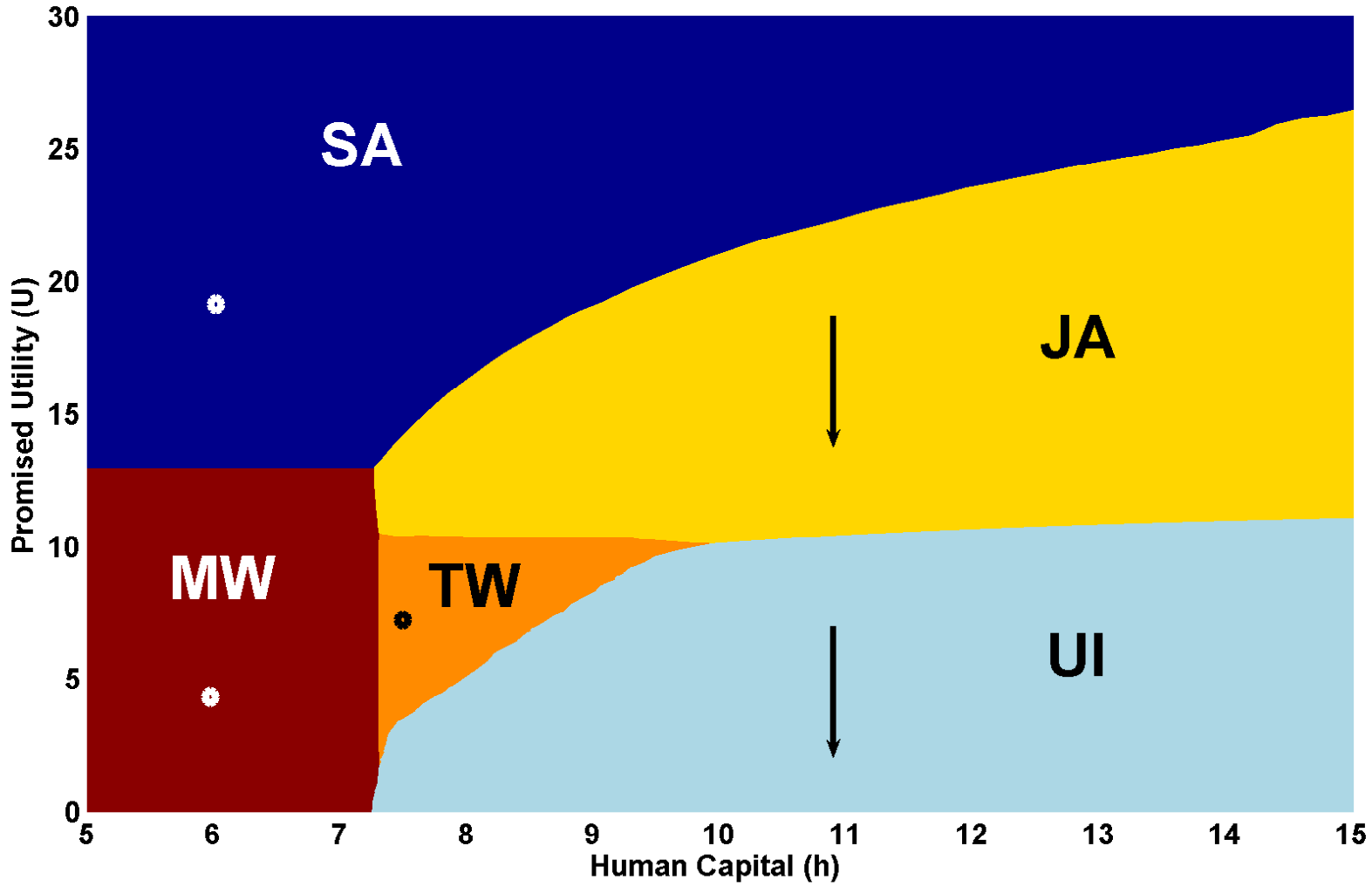
- Full **history dependence** allowed in the contract:  $U^f$  chosen
- Need to **convexify** the upper envelope  $V(U, h) = \max_i V^i(U, h)$ 
  - Phelan-Stachetti (2001)

# Dynamic incentives

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- Full **history dependence** allowed in the contract:  $U^f$  chosen
- Need to **convexify** the upper envelope  $V(U, h) = \max_i V^i(U, h)$ 
  - Phelan-Stachetti (2001)
- $U$  may change during unemployment spell
  - ▶ Never rises
  - ▶ Falls in policies with **IC binding**: UI and JA
  - ▶ Some **new policy transitions** due to dynamic incentives

# Optimal WTW program



## Three additional insights

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1. Policies with binding IC constraints (UI, JA) expand

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2. Only  $JA$  is a source of transitions

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3. Work requirement used as punishment for failed job-search:

- $\downarrow U^f$  achieved with future work effort requirements instead of  $\downarrow c$
- Better consumption smoothing

# 7. POLICY EVALUATION



# Policy Evaluation

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Aim: cost saving of switching from actual to optimal WTW program

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## 1. Parameterization

- Labor market parameters:  $e$ ,  $\pi$ , and  $h$  depreciation
- Costs and returns of technologies:  $\kappa^A$ ,  $(\underline{\omega}, \kappa^P)$ ,  $(\kappa^T, \theta, \bar{h})$ 
  - ▶ Evaluation studies of randomized experiments

# Policy Evaluation

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Aim: cost saving of switching from actual to optimal WTW program

## 1. Parameterization

- Labor market parameters:  $e$ ,  $\pi$ , and  $h$  depreciation
- Costs and returns of technologies:  $\kappa^A$ ,  $(\underline{\omega}, \kappa^P)$ ,  $(\kappa^T, \theta, \bar{h})$ 
  - ▶ Evaluation studies of randomized experiments

## 2. Expected utility ( $U_0$ ) and cost ( $K_0$ ) implied by current programs

- Benefits, time limits, sanctions, exemptions, policies

# Policy Evaluation

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Aim: cost saving of switching from actual to optimal WTW program

## 1. Parameterization

- Labor market parameters:  $e$ ,  $\pi$ , and  $h$  depreciation
- Costs and returns of technologies:  $\kappa^A$ ,  $(\underline{\omega}, \kappa^P)$ ,  $(\kappa^T, \theta, \bar{h})$ 
  - ▶ Evaluation studies of randomized experiments

## 2. Expected utility ( $U_0$ ) and cost ( $K_0$ ) implied by current programs

- Benefits, time limits, sanctions, exemptions, policies

## 3. Expected cost ( $K_0^*$ ) of optimal WTW program starting from $U_0$

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- $UI$  evaluated at a point  $(U, h^*)$  on the policy-indifference curve:

$$V^{UI}(U, h^*) = - \exp((1 - \beta)U) + \beta \left\{ \pi(h^*) W \left( U + \frac{e}{\beta \pi(h^*)}, h^* \right) + (1 - \pi(h^*)) \left[ (1 - \delta) V^{UI}(U, h^*) + \delta V(U, h'(h^*)) \right] \right\}$$

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- Compute the  $\max$  across policies at  $h'(h^*) < h^*$ :

$$\begin{aligned} V(U, h'(h^*)) & = \max \left\{ V^{UI}(U, h'(h^*)), V^{MW}(U) \right\} \\ & = V^{MW}(U) = V^{UI}(U, h^*) \end{aligned}$$



# 8. HIDDEN STORAGE

## Hidden storage

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### Sketch of proof:

- With  $R = \beta^{-1}$ , the agent's Euler Equation commands  $c_t = \mathbb{E}[c_{t+1}]$
- Payments are **weakly increasing** along the optimal WTW program
- Agent would like to borrow (and she can't), **never save**

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- Participation of non-employed TANF recipients

Activity	%
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Community Work	8.2
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- Generosity of US states towards TANF recipients

State	Max Monthly Benefits (family of three)	Time Limits (months)
New York	\$753	60
Massachussets	\$633	60
Arizona	\$278	36
Florida	\$303	48

## Digression: $u^{-1}$ convex first derivative?

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- $\frac{1}{u'}$  is the marginal cost to the planner of promising an additional unit of utility  $U$  to the agent
- **Definition [incentive cost]:** extra cost in units of consumption of promising the agent a state-contingent utility lottery delivering  $U$  necessary to satisfy IC, relative to the cost of promising  $U$  with certainty
- If  $\frac{1}{u'}$  is convex, then the incentive cost is increasing in  $U$
- CARA or CRRA ( $\gamma > 1/2$ )  $\Rightarrow \frac{1}{u'}$  convex